

## Chapter 17. Pythagoras Theorem

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### Ex 17.1

#### Answer 1.

Base = 5cm, Hypotenuse = 13cm

By Pythagoras theorem,

$$(\text{perpendicular})^2 = (13\text{cm})^2 - (5\text{cm})^2$$

$$(\text{perpendicular})^2 = 169\text{cm}^2 - 25\text{cm}^2$$

$$(\text{perpendicular})^2 = 144\text{cm}^2$$

$$(\text{perpendicular})^2 = (12\text{cm})^2$$

$$\therefore \text{perpendicular} = 12\text{cm}$$

Area of the triangle =  $\frac{1}{2} \times (\text{Base} \times \text{Perpendicular})$

$$= \frac{1}{2} \times 5\text{cm} \times 12\text{cm}$$

$$= 30\text{cm}^2$$

#### Answer 2.

The two sides (excluding hypotenuse) of a right - angled triangle are given as 24cm and 7cm

$$(\text{hypotenuse})^2 = (24\text{cm})^2 + (7\text{cm})^2$$

$$(\text{hypotenuse})^2 = 576\text{cm}^2 + 49\text{cm}^2$$

$$(\text{hypotenuse})^2 = 625\text{cm}^2$$

$$(\text{hypotenuse})^2 = (25\text{cm})^2$$

Thus, the length of the hypotenuse of the triangle is 25cm.

**Answer 3.**

Hypotenuse = 65cm

One side = 16cm

Let the other side be of length x cm

By Pythagoras theorem,

$$(65\text{cm})^2 = (16\text{cm})^2 + (x \text{ cm})^2$$

$$(x \text{ cm})^2 = 4225\text{cm}^2 - 256\text{cm}^2$$

$$= 3969\text{cm}^2$$

$$= (63\text{cm})^2$$

$$\Rightarrow x = 63\text{cm}$$

$$\text{Area of the triangle} = \frac{1}{2} \times (\text{Base} \times \text{Height})$$

$$= \frac{1}{2} \times 16\text{cm} \times 63\text{cm}$$

$$= 504 \text{ cm}^2$$

**Answer 4.**

Let O be the original position of the man.

From the figure, it is clear that B is the final position of the man.

$\triangle AOB$  is right - angled at A.

By Pythagoras theorem,

$$OB^2 = OA^2 + AB^2$$

$$OB^2 = (10\text{m})^2 + (24\text{m})^2$$

$$OB^2 = 100\text{m}^2 + 576\text{m}^2$$

$$OB^2 = 676\text{m}^2$$

$$OB^2 = (26\text{m})^2$$

$$OB = 26\text{m}$$

Thus, the man is at a distance of 26m from the starting point.

**Answer 5.**

Let AC be the ladder and A be the position of the window.

Then,  $AC = 25\text{m}$ ,  $AB = 20\text{m}$

Using Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow (25\text{m})^2 = (20\text{m})^2 + BC^2$$

$$\Rightarrow BC^2 = 625\text{m}^2 - 400\text{m}^2$$

$$BC^2 = 225\text{m}^2$$

$$BC^2 = (15\text{m})^2$$

$$\Rightarrow BC = 15\text{m}$$

Thus, the distance of the foot of the ladder from the building is 15m.

**Answer 6.**

Hypotenuse =  $p$  cm

One side =  $q$  cm

Let the length of the third side be  $x$  cm.

Using Pythagoras theorem,

$$x^2 = p^2 - q^2 = (p + q)(p - q)$$

$$= (p + q) \times 1 \quad [\because p - q = 1, \text{ given}]$$

$$= p + q$$

$$\therefore x = \sqrt{p + q}$$

Thus, the length of the third side of the triangle is  $\sqrt{p + q}$  cm.

### Answer 7.

Let O be the foot of the ladder. Let AO be the position of the ladder when it touches the window at A which is 9m high and CO be the position of the ladder when it touches the window at C which is 12m high.

Using Pythagoras theorem,

In  $\triangle AOB$ ,

$$BO^2 = AO^2 - AB^2$$

$$BO^2 = (15\text{m})^2 - (9\text{m})^2$$

$$BO^2 = 225\text{m}^2 - 81\text{m}^2$$

$$BO^2 = 144\text{m}^2$$

$$BO^2 = (12\text{m})^2$$

$$BO = 12\text{m}$$

Using Pythagoras theorem in  $\triangle COB$ ,

$$DO^2 = CO^2 - CD^2$$

$$DO^2 = (15\text{m})^2 - (12\text{m})^2$$

$$DO^2 = 225\text{m}^2 - 144\text{m}^2$$

$$DO^2 = 81\text{m}^2$$

$$DO = 9\text{m}$$

$$\text{Width of the street} = DO + BO = 9\text{m} + 12\text{m} = 21\text{m}$$

### Answer 8.

Let AC be the ladder and A be the position of the window which is 8m above the ground.

Now, the ladder is shifted such that its foot is at point D which is 8m away from the wall.

$$\therefore BD = 8\text{m}$$

At this instance, the position of the ladder is DE.

$$\therefore AC = DE$$

Using Pythagoras theorem in  $\triangle ABC$ ,

$$AC^2 = AB^2 + BC^2$$

$$= (8\text{m})^2 + (6\text{m})^2$$

$$= 64\text{m}^2 + 36\text{m}^2$$

$$= 100\text{m}^2$$

$$= (10\text{m})^2$$

$$\therefore AC = DE = 10\text{m}$$

Using Pythagoras theorem in  $\triangle DBE$ ,

$$\begin{aligned}BE^2 &= DE^2 - BD^2 \\ \Rightarrow BE^2 &= (10\text{m})^2 - (8\text{m})^2 \\ &= 100\text{m}^2 - 64\text{m}^2 \\ &= 36\text{m}^2 \\ &= (6\text{m})^2 \\ \Rightarrow BE &= 6\text{m}\end{aligned}$$

Thus, the required height up to which the ladder reaches is 6m above the ground.

### **Answer 9.**

Let AB and CD be the two poles of height 14m and 9m respectively.

It is given that  $BD = 12\text{m}$

$$\therefore CE = 12\text{m}$$

Now,  $AE = AB - BE$

$$= 14\text{m} - 9\text{m} = 5\text{m}$$

Using Pythagoras theorem in  $\triangle ACE$ ,

$$\begin{aligned}AC^2 &= AE^2 + CE^2 \\ &= (5\text{m})^2 + (12\text{m})^2 \\ &= 25\text{m}^2 + 144\text{m}^2 \\ &= 169\text{m}^2 \\ &= 13\text{m}^2 \\ \Rightarrow AC &= 13\text{m}\end{aligned}$$

Thus, the distance between the tops of the poles is 13m

### Answer 10.

It is given that the diagonals of a rhombus are of length 14cm and 10cm respectively

$$\therefore d_1 = 14\text{cm}, d_2 = 10\text{cm}$$

The diagonals of a rhombus bisect each other

$$\therefore \left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2 = \text{side}^2$$

$$\Rightarrow \text{side}^2 = 12^2 + 5^2 = 144 + 25 = 169$$

$$\Rightarrow \text{Side} = 13$$

Thus, each side of the rhombus is of length 13cm

### Answer 11.

Side of the rhombus = 10cm

One diagonal,  $d_1 = 16\text{cm}$

Let  $d_2$  be the other diagonal of the rhombus

The diagonals of a rhombus bisect each other

$$\therefore \left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2 = \text{side}^2$$

$$8^2 + \left(\frac{d_2}{2}\right)^2 = 100$$

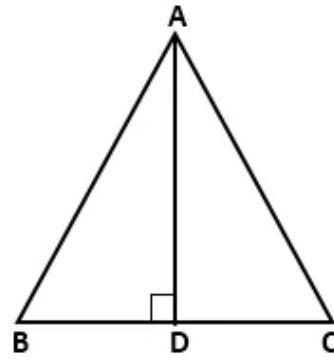
$$\Rightarrow \left(\frac{d_2}{2}\right)^2 = 100 - 64 = (6)^2$$

$$\Rightarrow \frac{d_2}{2} = 6$$

$$\Rightarrow d_2 = 12$$

Thus, the other diagonal of the rhombus is of length 12cm

**Answer 12.**



Since triangles ABD and ACD are right triangles right-angled at D,

$$AB^2 = AD^2 + BD^2 \quad \dots(i)$$

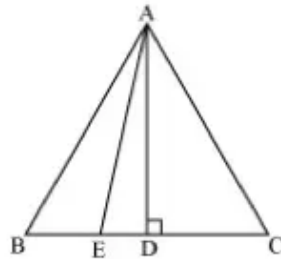
$$AC^2 = AD^2 + CD^2 \quad \dots(ii)$$

Subtracting (ii) from (i), we get

$$AB^2 - AC^2 = BD^2 - CD^2$$

$$\Rightarrow AB^2 + CD^2 = AC^2 + BD^2$$

**Answer 13.**



Let side of equilateral triangle be  $a$ . And  $AD$  be the altitude of  $\triangle ABC$

$$\text{So, } BE = EC = \frac{BC}{2} = \frac{a}{2}$$

$$\text{And, } AD = \frac{a\sqrt{3}}{2}$$

$$\text{Given that } BD = \frac{1}{3} BC = \frac{a}{3}$$

$$\text{So, } DE = BD - BE = \frac{a}{2} - \frac{a}{3} = \frac{a}{6}$$

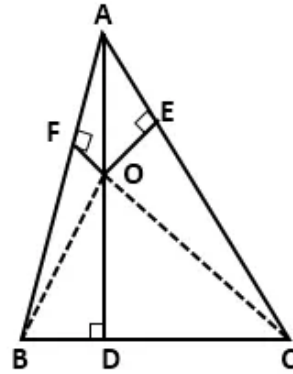
Now, in  $\triangle ADE$  by applying Pythagoras theorem

$$AD^2 = AE^2 + DE^2$$

$$\begin{aligned} AD^2 &= \left(\frac{a\sqrt{3}}{2}\right)^2 + \left(\frac{a}{6}\right)^2 \\ &= \left(\frac{3a^2}{4}\right) + \left(\frac{a^2}{36}\right) = \frac{28a^2}{36} \end{aligned}$$

$$\text{Or, } 9 AD^2 = 7 AB^2.$$

**Answer 14.**



a. In right triangles OFA, ODB and OEC, we have

$$OA^2 = AF^2 + OF^2$$

$$OB^2 = BD^2 + OD^2$$

$$OC^2 = CE^2 + OE^2$$

Adding all these results, we get

$$OA^2 + OB^2 + OC^2 = AF^2 + BD^2 + CE^2 + OF^2 + OD^2 + OE^2$$

$$\Rightarrow AF^2 + BD^2 + CE^2 = OA^2 + OB^2 + OC^2 - OD^2 - OE^2 - OF^2$$

b. In right triangles ODB and ODC, we have

$$OB^2 = OD^2 + BD^2$$

$$OC^2 = OD^2 + CD^2$$

$$\therefore OB^2 - OC^2 = (OD^2 + BD^2) - (OD^2 + CD^2)$$

$$\Rightarrow OB^2 - OC^2 = BD^2 - CD^2 \quad \dots(i)$$

Similarly, we have

$$OC^2 - OA^2 = CE^2 - AE^2 \quad \dots(ii)$$

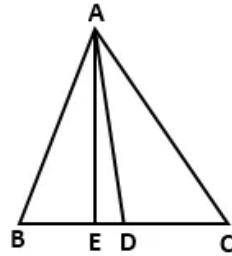
$$OA^2 - OB^2 = AF^2 - BF^2 \quad \dots(iii)$$

Adding (i), (ii) and (iii), we get

$$(OB^2 - OC^2) + (OC^2 - OA^2) + (OA^2 - OB^2) = (BD^2 - CD^2) + (CE^2 - AE^2) + (AF^2 - BF^2)$$

$$\Rightarrow (BD^2 + CE^2 + AF^2) - (AE^2 + CD^2 + BF^2) = 0$$

$$\Rightarrow AF^2 + BD^2 + CE^2 = AE^2 + CD^2 + BF^2$$

**Answer 15.**

We have  $\angle AED = 90^\circ$ ,

$\therefore \angle ADE < 90^\circ$  and  $\angle ADC > 90^\circ$

i.e.  $\angle ADE$  is acute and  $\angle ADC$  is obtuse.

a. In  $\triangle ADC$ ,  $\angle ADC$  is an obtuse angle.

$$\therefore AC^2 = AD^2 + DC^2 + 2 \times DC \times DE$$

$$\Rightarrow AC^2 = AD^2 + \left(\frac{1}{2}BC\right)^2 + 2 \times \frac{1}{2}BC \times DE$$

$$\Rightarrow AC^2 = AD^2 + \frac{1}{4}BC^2 + BC \times DE$$

$$\Rightarrow AC^2 = AD^2 + BC \times DE + \frac{1}{4}BC^2 \quad \dots(i)$$

b. In  $\triangle ABD$ ,  $\angle ADE$  is an acute angle.

$$\therefore AB^2 = AD^2 + BD^2 - 2 \times BD \times DE$$

$$\Rightarrow AB^2 = AD^2 + \left(\frac{1}{2}BC\right)^2 - 2 \times \frac{1}{2}BC \times DE$$

$$\Rightarrow AB^2 = AD^2 + \frac{1}{4}BC^2 - BC \times DE$$

$$\Rightarrow AB^2 = AD^2 - BC \times DE + \frac{1}{4}BC^2 \quad \dots(ii)$$

c. Adding (i) and (ii), we have

$$AC^2 + AB^2 = AD^2 + BC \times DE + \frac{1}{4}BC^2 + AD^2 - BC \times DE + \frac{1}{4}BC^2$$

$$\Rightarrow AB^2 + AC^2 = 2AD^2 + \frac{1}{2}BC^2 \quad \dots(iii)$$

d. Subtracting (ii) from (i), we have

$$AC^2 - AB^2 = AD^2 + BC \times DE + \frac{1}{4}BC^2 - AD^2 + BC \times DE - \frac{1}{4}BC^2$$

$$\Rightarrow AC^2 - AB^2 = 2BC \times DE$$

e. From (iii), we have

$$AB^2 + AC^2 = 2AD^2 + \frac{1}{2}BC^2$$

$$\Rightarrow AB^2 + AC^2 = 2AD^2 + \frac{1}{2}(2 \times CD)^2$$

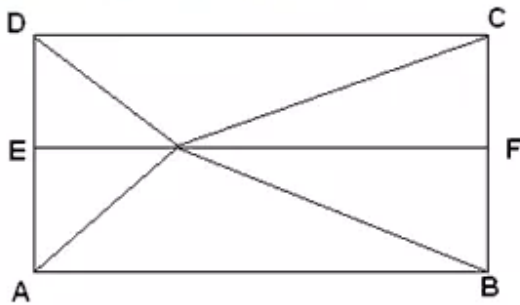
$$\Rightarrow AB^2 + AC^2 = 2AD^2 + \frac{1}{2} \times 4CD^2$$

$$\Rightarrow AB^2 + AC^2 = 2AD^2 + 2CD^2$$

$$\Rightarrow AB^2 + AC^2 = 2(AD^2 + CD^2)$$

**Answer 16.**

Let ABCD be the given rectangle and let O be a point within it.  
Join OA, OB, OC and OD.



Through O, draw EOF  $\parallel$  AB. Then, ABFE is a rectangle.

In right triangles  $\triangle OEA$  and  $\triangle OFC$ , we have

$$OA^2 = OE^2 + AE^2 \text{ and } OC^2 = OF^2 + CF^2$$

$$\Rightarrow OA^2 + OC^2 = (OE^2 + AE^2) + (OF^2 + CF^2)$$

$$\Rightarrow OA^2 + OC^2 = OE^2 + OF^2 + AE^2 + CF^2 \dots\dots(i)$$

Now, in right triangles  $\triangle OFB$  and  $\triangle ODE$ , we have

$$OB^2 = OF^2 + FB^2 \text{ and } OD^2 = OE^2 + DE^2$$

$$\Rightarrow OB^2 + OD^2 = (OF^2 + FB^2) + (OE^2 + DE^2)$$

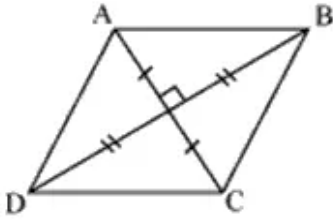
$$\Rightarrow OB^2 + OD^2 = OE^2 + OF^2 + DE^2 + BF^2$$

$$\Rightarrow OB^2 + OD^2 = OE^2 + OF^2 + CF^2 + AE^2 [\because DE = CF \text{ and } AE = BF] \dots\dots(ii)$$

From (i) and (ii), we get

$$OA^2 + OC^2 = OB^2 + OD^2$$

**Answer 17.**



In  $\triangle AOB, \triangle BOC, \triangle COD, \triangle AOD$

Applying Pythagoras theorem

$$AB^2 = AO^2 + OB^2$$

$$BC^2 = BO^2 + OC^2$$

$$CD^2 = CO^2 + OD^2$$

$$AD^2 = AO^2 + OD^2$$

Adding all these equations,

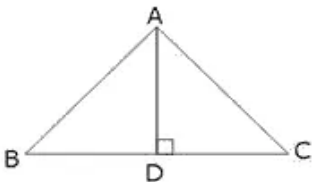
$$AB^2 + BC^2 + CD^2 + AD^2 = 2(AO^2 + OB^2 + OC^2 + OD^2)$$

$$= 2\left[\left(\frac{AC}{2}\right)^2 + \left(\frac{BD}{2}\right)^2 + \left(\frac{AC}{2}\right)^2 + \left(\frac{BD}{2}\right)^2\right] \quad (\text{diagonals bisect each other.})$$

$$= 2\left[\frac{(AC)^2}{2} + \frac{(BD)^2}{2}\right]$$

$$= (AC)^2 + (BD)^2$$

**Answer 18.**



In equilateral triangle  $AD \perp BC$ .

$$\Rightarrow BD = DC = \frac{BC}{2} \quad (\text{In equilateral triangle altitude bisects the opposite side})$$

In right triangle  $ABD$ ,

$$AB^2 = AD^2 + BD^2$$

$$= AD^2 + \left(\frac{BC}{2}\right)^2$$

$$= \frac{4AD^2 + BC^2}{4}$$

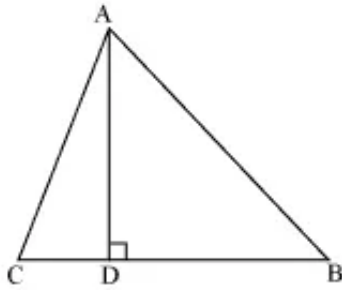
$$= \frac{4AD^2 + AB^2}{4} \quad (\text{Since } AB = BC)$$

$$\Rightarrow 4AB^2 = 4AD^2 + AB^2$$

$$\Rightarrow 3AB^2 = 4AD^2$$

Hence proved.

**Answer 19.**



In  $\triangle ACD$

$$AC^2 = AD^2 + DC^2$$

$$AD^2 = AC^2 - DC^2 \quad (1)$$

In  $\triangle ABD$

$$AB^2 = AD^2 + DB^2$$

$$AD^2 = AB^2 - DB^2 \quad (2)$$

From equation (1) and (2)

$$\text{Therefore } AC^2 - DC^2 = AB^2 - DB^2$$

since given that  $3DC = DB$

$$DC = \frac{BC}{4} \text{ and } DB = \frac{3BC}{4}$$

$$AC^2 - \left(\frac{BC}{4}\right)^2 = AB^2 - \left(\frac{3BC}{4}\right)^2$$

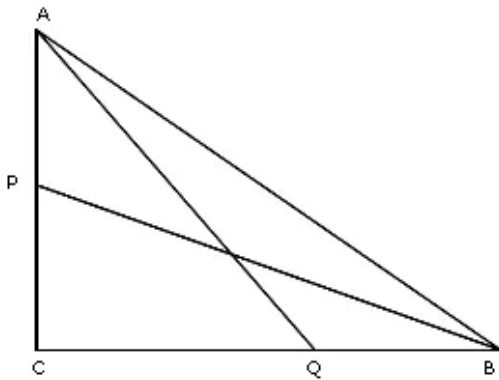
$$AC^2 - \frac{BC^2}{16} = AB^2 - \frac{9BC^2}{16}$$

$$16AC^2 - BC^2 = 16AB^2 - 9BC^2$$

$$\Rightarrow 16AB^2 - 16AC^2 = 8BC^2$$

$$\Rightarrow 2AB^2 = 2AC^2 + BC^2$$

**Answer 20.**



P divides AC in the ratio 2 : 1

$$\text{So } CP = \frac{2}{3} AC \dots\dots(i)$$

Q divides BC in the ratio 2: 1

$$QC = \frac{2}{3} BC \quad \dots\dots (ii)$$

(i) In  $\Delta ACQ$

Using Pythagoras Theorem we have,

$$AQ^2 = AC^2 + CQ^2$$

$$\Rightarrow AQ^2 = AC^2 + \frac{4}{9}BC^2 \quad (\text{using (ii)})$$

$$\Rightarrow 9AQ^2 = 9AC^2 + 4BC^2 \quad \dots\dots(iii)$$

(ii) Applying Pythagoras theorem in right triangle BCP, we have

$$BP^2 = BC^2 + CP^2$$

$$\Rightarrow BP^2 = BC^2 + \frac{4}{9} AC^2 \quad (\text{Using (i)})$$

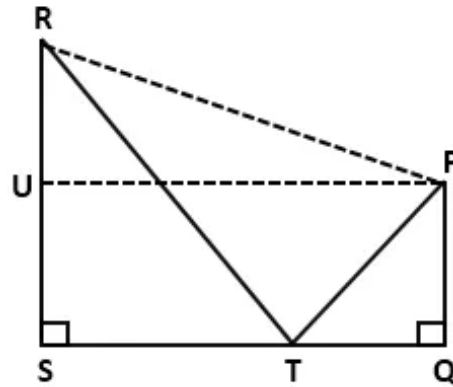
$$\Rightarrow 9BP^2 = 9BC^2 + 4AC^2$$

Adding (iii) and (iv), we get

$$9(AQ^2 + BP^2) = 13(BC^2 + AC^2)$$

$$\Rightarrow 9(AQ^2 + BP^2) = 13 AB^2$$

**Answer 21.**



$$PQ = \frac{RS}{3} = 8 \text{ cm}$$

$$\Rightarrow PQ = 8 \text{ cm and } RS = 3 \times 8 = 24 \text{ cm}$$

$$3ST = 4QT = 48 \text{ cm}$$

$$\Rightarrow ST = \frac{48}{3} = 16 \text{ cm and } QT = \frac{48}{4} = 12 \text{ cm}$$

In  $\Delta PTQ$ ,

$$PT^2 = PQ^2 + QT^2 = 8^2 + 12^2 = 64 + 144 = 208$$

In  $\Delta RTS$ ,

$$RT^2 = RS^2 + ST^2 = 24^2 + 16^2 = 576 + 256 = 832$$

$$\text{Now, } PT^2 + RT^2 = 208 + 832 = 1040 \quad \dots(i)$$

Draw  $PU \perp RS$  and Join  $PR$ .

$$PU = SQ = ST + TQ = 16 + 12 = 28 \text{ cm}$$

$$RU = RS - US = RS - PQ = 24 - 8 = 16 \text{ cm}$$

In  $\Delta RUP$ ,

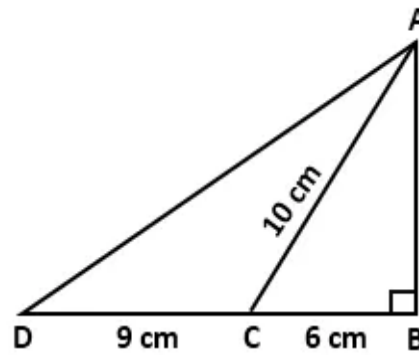
$$PR^2 = RU^2 + PU^2 = 16^2 + 28^2 = 256 + 784 = 1040 \quad \dots(ii)$$

From (i) and (ii), we get

$$PT^2 + RT^2 = PR^2$$

Thus,  $\angle RTP = 90^\circ$

**Answer 22.**



In  $\triangle ABC$ ,  $\angle B = 90^\circ$

$$\therefore AC^2 = AB^2 + BC^2 \quad \dots(\text{Pythagoras Theorem})$$

$$\Rightarrow 10^2 = AB^2 + 6^2$$

$$\Rightarrow AB^2 = 10^2 - 6^2 = 100 - 36 = 64$$

Now,  $BD = BC + CD = 6 + 9 = 15$  cm

$$\Rightarrow BD^2 = 225$$

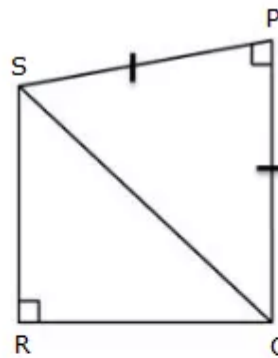
In  $\triangle ABD$ ,  $\angle B = 90^\circ$

$$\therefore AD^2 = AB^2 + BD^2$$

$$\Rightarrow AD^2 = 64 + 225 = 289$$

$$\Rightarrow AD = 17 \text{ cm}$$

**Answer 23.**



In  $\triangle SRQ$ ,  $\angle R = 90^\circ$

$$\therefore QS^2 = RS^2 + QR^2 \quad \dots(\text{Pythagoras Theorem})$$

$$= 20^2 + 21^2$$

$$= 400 + 441$$

$$= 841$$

Now, in  $\triangle QSP$ ,  $\angle P = 90^\circ$

$$\therefore QS^2 = PQ^2 + PS^2 \quad \dots(\text{Pythagoras Theorem})$$

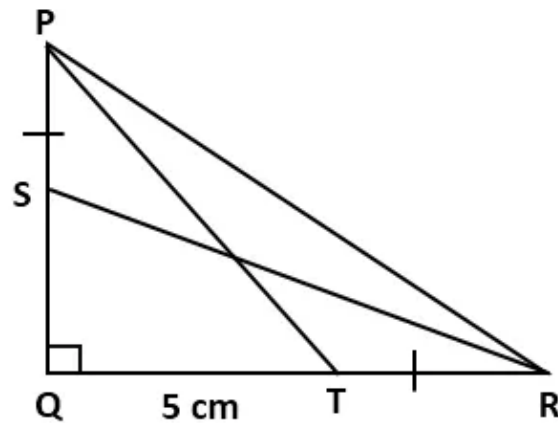
$$\Rightarrow QS^2 = PQ^2 + PQ^2 \quad \dots(\text{Given } PQ = PS)$$

$$\Rightarrow QS^2 = 2PQ^2$$

$$\Rightarrow PQ^2 = \frac{QS^2}{2} = \frac{841}{2} = 420.5$$

$$\Rightarrow PQ = 20.50 \text{ cm}$$

**Answer 24.**



In  $\Delta PQT$ ,  $\angle Q = 90^\circ$

$\therefore PT^2 = PQ^2 + QT^2$  ....(By Pythagoras Theorem)

$$\Rightarrow PQ^2 = PT^2 - QT^2 = 13^2 - 5^2 = 169 - 25 = 144$$

$$\Rightarrow PQ = 12 \text{ cm}$$

Now,  $PS = TR = a$ (say)

In  $\Delta SQR$ ,  $\angle Q = 90^\circ$

$\therefore SR^2 = QS^2 + QR^2$  ....(By Pythagoras Theorem)

$$\Rightarrow SR^2 = (PQ - PS)^2 + (QT + TR)^2$$

$$\Rightarrow SR^2 = (PQ - PS)^2 + (QT + PS)^2 \quad \dots\text{.(Since } PS = TR\text{)}$$

$$\Rightarrow SR^2 = PQ^2 - 2 \times PQ \times PS + PS^2 + QT^2 + 2 \times QT \times PS + PS^2$$

$$\Rightarrow 13^2 = 12^2 - 2 \times 12 \times a + a^2 + 5^2 + 2 \times 5 \times a + a^2$$

$$\Rightarrow 169 = 144 - 24a + a^2 + 25 + 10a + a^2$$

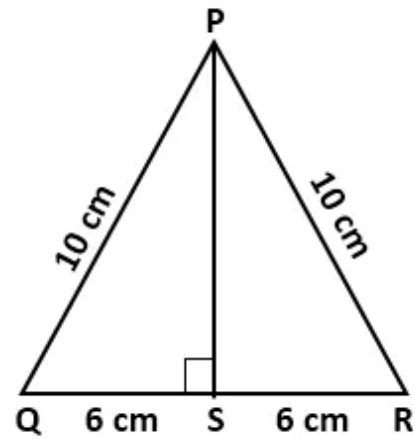
$$\Rightarrow 169 = 169 - 14a + 2a^2$$

$$\Rightarrow 2a^2 = 14a$$

$$\Rightarrow a = 7$$

Hence,  $PS = 7 \text{ cm}$

**Answer 25.**



Since, PQR is an isosceles triangle and  $PS \perp QR$ , therefore it divides QR into two equal parts.

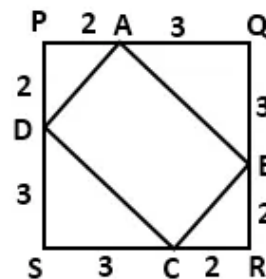
In  $\triangle PSQ$ ,  $\angle S = 90^\circ$

$\therefore PQ^2 = PS^2 + QS^2$  ....(By Pythagoras Theorem)

$$\Rightarrow PS^2 = PQ^2 - QS^2 = 10^2 - 6^2 = 100 - 36 = 64$$

$$\Rightarrow PS = 8 \text{ cm}$$

**Answer 26.**



In  $\triangle APD$ ,  $\angle P = 90^\circ$

$$\therefore AD^2 = AP^2 + PD^2 = 2^2 + 2^2 = 4 + 4 = 8$$

$$\Rightarrow AD = 2\sqrt{2} \text{ cm}$$

Similarly, we can prove that in  $\triangle BRC$ ,

$$BC = 2\sqrt{2} \text{ cm}$$

$$\therefore AD = BC \quad \dots(i)$$

In  $\triangle AQB$ ,  $\angle Q = 90^\circ$

$$\therefore AB^2 = AQ^2 + BQ^2 = 3^2 + 3^2 = 9 + 9 = 18$$

$$\Rightarrow AB = 3\sqrt{2} \text{ cm}$$

Similarly, we can prove that in  $\triangle CSD$ ,

$$CD = 3\sqrt{2} \text{ cm}$$

$$\therefore AB = CD \quad \dots(ii)$$

Again, in  $\triangle APD$ ,

$$AP = PD$$

$$\Rightarrow \angle PAD = \angle PDA = 45^\circ$$

Also, in  $\triangle AQB$ ,

$$AQ = BQ$$

$$\Rightarrow \angle QAB = \angle QBA = 45^\circ$$

$$\text{Now, } \angle PAD + \angle DAB + \angle QAB = 180^\circ$$

$$\Rightarrow 45^\circ + \angle DAB + 45^\circ = 180^\circ$$

$$\Rightarrow \angle DAB = 90^\circ$$

Similarly, we can prove that  $\angle ABC$ ,  $\angle BCD$  and  $\angle ADC$  are  $90^\circ$  each.

Thus, ABCD is a rectangle as opposite sides are equal and each angle is  $90^\circ$ .

Now,

$$\text{Area of a rectangle ABCD} = AD \times AB = 2\sqrt{2} \times 3\sqrt{2} = 12 \text{ cm}^2$$

$$\text{Perimeter of a rectangle ABCD} = AB + BC + CD + AD$$

$$= 2\sqrt{2} + 3\sqrt{2} + 2\sqrt{2} + 3\sqrt{2}$$

$$= 10\sqrt{2} \text{ cm}$$